

05/26/99  
JC594 U.S. PTO

A

PATENT

Docket No. D-362

Commissioner of Patents and Trademarks  
Washington, D.C. 20231

**NEW APPLICATION TRANSMITTAL**

Transmitted herewith for filing is the patent application of

Inventor(s): Philip A. Dafesh and Tien M. Nguyen

JC594 U.S. PTO  
05/26/99  
09/318560

For (title): Quadrature Product Subcarrier Modulation Method

**1. Type of Application**

This new application is an ORIGINAL application.

**2. Benefit of Prior U.S. Application(s) (35 USC 120) - None**

**CERTIFICATION UNDER 37 CFR 1.10**

I hereby certify that this New Application Transmittal and the documents referred to as enclosed therein are being deposited with the United States Postal Service on this date May 26, 1999 in an envelope as "Express Mail Post Office to Addressee" Mailing Label Number EE257872748US addressed to the: Commissioner of Patents and Trademarks, Washington, D.C. 20231

Carole A. Mulchinski  
(Type or print name of person mailing paper)  
Carole A. Mulchinski  
(Signature of person mailing paper)

(Application Transmittal [4-1]--page 1 of 4)

**3. Papers Enclosed Which Are Required for Filing Date Under 37 CFR 1.53(b) (Regular) or  
37 CFR 1.153 (Design) Application**

40 Pages of specification  
15 Pages of claims  
1 Pages of Abstract  
3 Sheets of drawing

informal  
 in triplicate

**4. Additional papers enclosed**

Petition and Declaration under 37 CFR 1.47.  
 Information Disclosure Statement  
 Form PTO-1449  
 Small Entity Statement

**5. Declaration or oath executed by INVENTOR(S)**

Enclosed

**Inventorship Statement**

The inventorship for all the claims in this application is THE SAME.

**7. Language:** ENGLISH

**8. Assignment**

An assignment of the invention to The Aerospace Corporation  
P. O. Box 92957 (M1/040), Los Angeles, CA 90009-2957

is attached  
 will follow

**9. Certified Copy**

Certified copy(ies) of application(s) X are not applicable        are  
attached        will follow.

(Application Transmittal [4-1]-- page 2 of 4)

10. **Fee Calculation**

Regular application

**CLAIMS AS FILED**

Number Filed	Number Extra	Rate	Basic Fee
Total Claims	- 20 -20= 0	X \$ 18.00	\$760.00
Independent Claims	- 3 -3= 1	X \$ 39.00	00.00
Multiple dependent claim(s), if any			\$260.00

Amendment cancelling extra claims enclosed

Amendment deleting multiple dependencies enclosed

Fee for extra claims is not being paid at this time

Filing Fee Calculation **\$760.00**

11. **Small Entity Statement(s)**

Verified Statement(s) that this is a filing by a small entity under 37 CFR 1.9 and 1.27 is(are) attached.

**\$380.00**

12. **Fee Payment Being Made At This Time**

No filing fee is to be paid at this time. (This and the surcharge required by 37 CFR 1.16(e) can be paid subsequently.)

Enclosed

Basic filing fee **\$ 380.00**

Recording assignment (\$40.00; 37 CFR 1.21(h)(1)) **\$ 40.00**

**Total fees enclosed \$ 420.00**

(Application Transmittal [4-1]--page 3 of 4)

13. *Method of Payment of Fees*

charge Account No. 01-0428 in the amount of \$ 420.00.  
A duplicate of this transmittal is attached.

14. *Authorization to Charge Additional Fees*

The Commissioner is hereby authorized to charge the following additional fees by this paper and during the entire pendency of this application to Account No. 01-0428.

37 CFR 1.16 (filing fees)

37 CFR 1.16 (presentation of extra claims)

37 CFR 1.16(e) (surcharge for filing the basic filing fee and/or declaration on a date later than the filing date of the application)

37 CFR 1.17 (application processing fees)

37 CFR 1.18 (issue fee at or before mailing of Notice of Allowance, pursuant to 37 CFR 1.311(b)).

15. *Instructions As To Overpayment*

credit Account No. 01-0428.

Reg. No.: 32,096

  
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THE AEROSPACE CORPORATION  
P.O. Box 92957 (M1/040)  
Los Angeles, CA 90009-2957

This transmittal ends with this page.

(Application Transmittal [4-1]--page 4 of 4)

Applicant or Patentee: Philip A. Dafesh and Tien M. Nguyen

Serial or Patent No.: \_\_\_\_\_

Filed or Issued: \_\_\_\_\_

For: QUADRATURE PRODUCT SUBCARRIER MODULATION METHOD

**VERIFIED STATEMENT (DECLARATION) CLAIMING SMALL ENTITY STATUS (37 CFR 1.9(f) and 1.27(d))--NONPROFIT ORGANIZATION**

I hereby declare that I am an official empowered to act on behalf of the nonprofit organization identified below:

NAME OF ORGANIZATION The Aerospace Corporation

ADDRESS OF ORGANIZATION P. O. Box 92957 (M1/040)

Los Angeles, CA 90009-2957

**TYPE OF ORGANIZATION**

TAX EXEMPT UNDER INTERNAL REVENUE SERVICE CODE (26 USC 501 (a) and 501 (c) (3))

I hereby declare that the nonprofit organization identified above qualifies as a nonprofit organization as defined in 37 CFR 1.9(e) for purposes of paying reduced fees under Section 41(a) and (b) of Title 35, United States Code with regard to the invention entitled QUADRATURE PRODUCT SUBCARRIER MODULATION METHOD

by inventor(s) Philip A. Dafesh and Tien M. Nguyen

described in

the specification filed herewith

application serial No. \_\_\_\_\_, filed \_\_\_\_\_.

I hereby declare that rights under contract or law have been conveyed to and remain with the nonprofit organization with regard to the above identified invention.

If the rights held by the nonprofit organization are not exclusive, each individual, concern or organization having rights to the invention is listed and no rights to the invention are held by any person, other than the inventor, who could not qualify as a small business concern under 37 CFR 1.9(d) or by any concern which would not qualify as a small business concern under 37 CFR 1.9(d) or a nonprofit organization under 37 CFR 1.9(e).

I acknowledge the duty to file, in this application or patent, notification of any charge in status resulting in loss of entitlement to small entity status prior to paying, or at the time of paying, the earliest of the issue fee or any maintenance fee due after the date on which status as a small entity is no longer appropriate. (37 CFR 1.28(b))

I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section 1001 of Title 18 of the United States Code, and that such willful false statements may jeopardize the validity of the application, any patent issuing thereon, or any patent to which this verified statement is directed.

NAME OF PERSON SIGNING Robert Donald Matthews

TITLE IN ORGANIZATION Assistant General Counsel

ADDRESS OF PERSON SIGNING The Aerospace Corporation

P. O. Box 92957 (M1/040), Los Angeles, CA 90009-2957

SIGNATURE Robert Donald Matthews DATE May 26, 1999

1                   PATENT APPLICATION

2  
3                   Docket No.: D-362

4  
5                   Inventors: Philip A. Dafesh and Tien M. Nguyen

6  
7                   Quadrature Product Subcarrier Modulation System

8  
9                   SPECIFICATION

10  
11                  Statement of Government Interest

12  
13                  The invention was made with Government support under  
14                  contract No. F04701-93-C-0094 by the Department of the Air Force.  
15                  The Government has certain rights in the invention.

16  
17                  Reference to Related Application

18  
19                  The present application is related to applicant's copending  
20                  application entitled Coherent Adaptive Subcarrier Modulation  
21                  Method, S/N: xx/xxx,xxx, filed yy/yy/yy, by one of the named  
22                  inventors.

23                  Field of the Invention

24  
25                  The invention relates to the field of modulation of signals  
26                  of communication systems. More particularly, the present  
27                  invention relates to subcarrier modulation methods for efficient  
28                  frequency reuse within existing bandwidths.

## Background of the Invention

3        Due to the limited availability of spectrum allocations for  
4        communications systems, it has become desirable to reuse existing  
5        spectrum by employing bandwidth efficient modulation methods to  
6        existing satellite communications systems. In particular, it has  
7        become desirable to add new signals to existing quadrature  
8        multiplexed spread-spectrum communication signals, such as the  
9        signals employed in the Global Positioning System (GPS), within  
10      the existing spectral allocation. As the number of users of a  
11      given communication system increases, it is often desirable to  
12      augment the system with additional communication signals. One  
13      method that has been used to achieve this goal in timing,  
14      telemetry and command links is conventional subcarrier phase  
15      modulation. Furthermore, it is often necessary to modulate new  
16      signals onto existing quadrature multiplexed communication  
17      systems within the existing spectral allocation. It is desirable  
18      that any such approach satisfy various constraints, including  
19      causing minimal distortion of existing signals, transmitting new  
20      signals through the same high power amplifier used by existing  
21      signals, accommodating new data messages and new pseudo random  
22      noise (PRN) code families for spread-spectrum systems, providing  
23      flexibility to control the spectral separation of signals within  
24      the allocated band, and providing flexibility to control the  
25      distribution of energy in and outside of the allocated band.  
26      Unfortunately, for an existing quadrature-multiplexed  
27      communication systems having data modulations on both the I and Q  
28      channels, that is, the in-phase channel with zero degree phase

1 offset from the carrier, and the quadrature channel with ninety  
2 degree phase offset from the carrier, adding another signal  
3 slightly offset in frequency gives rise to a non-constant  
4 envelope that causes distortion to the existing signals when the  
5 total waveform is passed through a non-linear amplifier. For  
6 non-quadrature-multiplexed communication systems, the subcarrier  
7 modulation method has been employed to permit the realization of  
8 a constant-envelope modulation. Unfortunately, a general  
9 approach for applying the subcarrier modulation method to  
10 quadrature-modulated communication systems has not been  
11 previously developed.

12

13 GPS is undergoing a transformation with the Block IIF  
14 satellite. This redefinition of GPS from a military service with  
15 the guarantee of civil use to a true dual service is one of the  
16 GPS modernization goals. The transformation started out as a  
17 modest upgrade that involved a new civil L5 frequency and a  
18 military acquisition signal at the L2 frequency but has evolved  
19 into a complement of new signals at L1 and L2 frequencies for  
20 enhanced military and civil use. It is desirable to design and  
21 choose optimum M-code military signals and signal modulation  
22 methods that achieve better than current performances without  
23 degrading the existing signals. Under consideration are two  
24 classes of signals, the Manchester code signals and the binary  
25 offset carrier signals. These signals result from modulation of  
26 a non-return to zero pseudo random noise spreading code by a  
27 square-wave subcarrier. The Manchester code signal is a special  
28 case where the bit rate of the spreading code and the frequency

of the square-wave are the same. It is also equivalent to a Manchester encoded PRN code. The binary offset carrier signal has been defined as encompassing all the other cases where the rate of the spreading code is less than the subcarrier frequency. These signals share the characteristic of conventional subcarrier modulation that the waveform exhibits a null at the carrier frequency due to the square-wave subcarrier, and therefore, can allow for the transmission of the new GPS military M-codes along with the course acquisition C/A-codes, and precision P(Y) codes, where (Y) denotes the encrypted form of the P-code. One of the key challenges for a new signal scheme for the GPS transmitter is to transmit the C/A, P(Y), and M-code signals using a flexible efficient, constant envelope modulation method, compatible with goals of the GPS modernization.

To this end, it is desirable to develop a general high-efficiency constant-envelope subcarrier modulation approach to enable quadrature multiplexing of an M-code signal or signals onto the L1 and L2 GPS carriers that is applicable to both a combined-aperture for transmitting C/A, P(Y), and M-code signals through the same upconverter and amplifier chain and antenna, and a separate-aperture for transmitting M-code signals out of a separate upconverter, amplifier chain and antenna from C/A and P(Y) signals without resulting in significant signal loss due to inefficient signal modulation methods. The current Block II and Block IIR satellites employ constant-envelope quadrature multiplexing of two bi-phase modulated ranging code signals at the GPS L1 frequency, namely the C/A code and P(Y) code. The

1 baseline Block IIF satellite will also transmit these signals on  
2 both the GPS L1 and L2 frequencies, along with the new military  
3 signals.

4

5       The new M-code signal consists of the product of a military  
6 data modulation multiplied by a spreading code modulation.  
7 Previously proposed approaches for augmenting the existing GPS  
8 waveform, with a new split-spectrum M-code signal, such as the  
9 tri-code hexaphase modulation method, involve the linear addition  
10 of a single new M-code signal on to the existing GPS waveform.  
11 These approaches multiplex the additional signal with an existing  
12 I/Q quadrature modulation by adding a third signal to one of the  
13 I and Q phases. Unfortunately, this gives rise to the  
14 undesirable non-constant envelope, that is, a variable amplitude.  
15 For this case, the envelope of the composite signal is no longer  
16 constant due to the presence of the time-varying amplitude  
17 component in addition to the constant component of the envelope.  
18 This result is undesirable because the amplitude variations will  
19 give rise to AM-to-AM and AM-to-PM distortions when the signal is  
20 passed through a nonlinear amplifier unless the operating point  
21 of the amplifier is backed off from its saturation point to the  
22 linear region of amplifier operation. Such a back off can result  
23 in appreciable power losses.

24

25       During the course of the GPS military signal development  
26 study, a number of M-code signal modulation methods have been  
27 proposed. Two of the leading approaches were hard-limiting the  
28 sum of the C/A, P and M-code signals, and majority voting. The

hard-limiting approach involves forcing the non-constant envelope waveform resulting from the sum of C/A and M on one carrier phase and P on the other, to be constant by limiting the amplitude variation to a minimum value. This technique results in significant signal power loss and distortion for the case of equal C/A and M-code power levels as is the case for hard-limited tri-code hexaphase modulation method. Furthermore, the exact efficiency is critically related to the power balance between C/A, P(Y) and M-code signals and the desired balance between signals is not easy to achieve. An alternative approach to combining M-code with C/A and P(Y) code signals is through majority vote combining. In the majority vote approach, signals are time multiplexed, that is, time-shared, on either I or Q phases to allow multiple signals to be transmitted in a single constant envelope. The disadvantage of this approach results from the relatively large majority combining loss per code in combination, assuming equal power levels for all codes in the majority combination. Furthermore, it is difficult to control the relative power levels of the combined signals without incurring additional combining losses.

Conventional subcarrier modulation has been recognized as a means to modulate additional signals onto a modulated carrier signal while maintaining a constant envelope. The Space-Ground-Link Subsystem for example, employs three subcarriers that are phase-modulated onto a carrier signal to enable the modulation of four signals, including one carrier modulation and three subcarrier modulations. The classical

1 subcarrier approach, applied to non-quadrature-multiplexed  
2 communication systems, involves the phase-modulation of a carrier  
3 signal by one or more periodic subcarriers that are typically  
4 sine-wave, square-wave or triangle-wave signals. In this  
5 classical subcarrier approach, the range of the phase modulation  
6 is determined by a so-called modulation index, usually controlled  
7 by the gain of the phase modulator. In conventional subcarrier  
8 systems, cross-product intermodulation components of the waveform  
9 are interpreted as signal losses. A variation of conventional  
10 subcarrier modulation applicable to augmenting the existing GPS  
11 signals with new M-code signals is desirable due to the  
12 inefficiency of the previously proposed M-code signal combining  
13 techniques, that is, signal modulation methods.

14 An alternative combining method has been proposed to add the  
15 new M-code signals by spatially combining the new M-code signal  
16 with the C/A and P(Y) code signals by transmitting the new M-code  
17 signals through a separate antenna and amplifier chain. While  
18 this approach would, in principal, allow for the transmission of  
19 C/A-codes and P(Y)-codes within the M-code, the simplification in  
20 modulator design is more than offset by the impact on the  
21 satellite when adding an independent antenna and amplifier chain.  
22 Due to potential implementation difficulties with the  
23 separate-aperture approach, and a requirement to efficiently  
24 transmit the new M-code signals with world-wide coverage, the  
25 more challenging problem of transmitting these signals is the  
26 development of a general modulation approach to enable the  
27 transmission of these signals through a single modulator,  
28 upconverter, power amplifier chain and antenna aperture.

1       The leading modulation methods, that have been proposed thus  
2 far to achieve this end, have a maximum efficiency limited to  
3 roughly seventy-one percent in the allocated GPS spectral band.  
4 Efficiency is defined as the sum of the effective transmitter  
5 power after reception plus any band limiting losses and other  
6 losses associated with this sum divided by the total transmitted  
7 power. At the same time, the leading approaches with the highest  
8 efficiency restrict options available to optimize the waveform by  
9 transmitting a single M-code signal used for both acquisition and  
10 tracking.

11  
12       These single M-code approaches include tri-code hexaphase,  
13 hard-limited tri-code hexaphase, majority vote code multiplexing,  
14 and offset carrier and binary offset carrier modulations. The  
15 tri-code hexaphase, offset carrier and binary offset carrier  
16 modulation approaches have a non-constant envelope. As a result,  
17 these approaches cause distortion to existing signals when the  
18 total waveform is passed through a non-linear amplifier. The  
19 majority vote modulation approach employs a constant envelope but  
20 does not provide significant spectral separation and has limited  
21 inherent flexibility in adjusting the amplitude of generated  
22 harmonics. The majority vote modulation approach also suffers  
23 from majority combining losses that results in relatively poor  
24 overall power efficiency. The same is true for the hard-limited  
25 tri-code hexaphase modulation method.

26  
27       The transmission of both data and spreading code modulations  
28 in a quadrature-multiplexed communication channel is well known.

1 Conventional quadrature phase shift keying (QPSK) direct-sequence  
2 spread spectrum modulation schemes generally employ spreading  
3 sequences on the in-phase and quadrature channels. The  
4 modulation of unspread data is a special case. For GPS L1 or L2  
5 carriers modulated by codes and data, a carrier signal is  
6 modulated by codes and data in a conventional quadrature  
7 modulated communication signal as  $S_0(t)$  in terms of the in-phase  
8  $I_0(t)$  and quadrature  $Q_0(t)$  signals. The signal  $S_0(t)$  can express  
9 GPS L1 and L2 carriers modulated by C/A and P codes and data in a  
10 conventional quadrature modulation communication method in terms  
11 of an  $S_0(t)Q_0/I_0$  equation with respect to an  $I_0$  equation and a  $Q_0$   
12 equation.

13

14

15  $S_0(t) = I_0(t) \cos(\omega_c t) - Q_0(t) \sin(\omega_c t)$

16

17

18

19  $I_0(t) = \sqrt{\frac{2P_I}{P_T}} D_I(t) C_I(t)$

20

21

22

23

24  $Q_0(t) = \sqrt{\frac{2P_Q}{P_T}} D_Q(t) C_Q(t)$

25

26

27

28

1       The  $C_I(t)$  and  $D_I(t)$  terms are the in-phase pseudo random  
2 noise spreading code and data modulation, and  $C_Q(t)$  and  $D_Q(t)$  are  
3 the quadrature pseudo random noise spreading code and data  
4 modulations.  $P_I$  and  $P_Q$  are the average power of the I and Q  
5 signals in relation to total power  $P_T$ .

6  
7       The signal  $S_0(t)$  may also be expressed in an  $S_0(t)A_0/\phi$   
8 equation. An  $A_0(t)$  magnitude equation describes the envelope form  
9 where  $A_0(t)$  is the magnitude envelope of  $S_0(t)$ . A  $\phi(t)$  equation  
10 describes the phase of  $S_0(t)$ .

11  
12       
$$S_0(t) = A_0(t) \cos(w_C t + \phi(t))$$

13  
14  
15       
$$A_0(t) = \sqrt{I_0^2(t) + Q_0^2(t)} = \sqrt{\frac{2(P_I + P_Q)}{P_T}} = \text{CONSTANT}$$

16  
17  
18       
$$\phi(t) = \tan^{-1} \frac{Q_0(t)}{I_0(t)} = \tan^{-1} \sqrt{\frac{P_Q}{P_I} \cdot \frac{D_Q(t) C_Q(t)}{D_I(t) C_I(t)}}$$

21  
22  
23       The total average power may be described by a  $P_{TF}$  equation  
24 for the signal  $S_0(t)$  that can be expressed by the magnitude of the  
25 envelope squared divided by two, in reference to identity  
26 equations based on the square of the  $C_I$  and  $C_Q$  code signals and  
27 the  $D_I$  and  $D_Q$  data signals.

$$P_{TF} = \frac{A_0^2}{2} = \frac{I_0^2 + Q_0^2}{2} = \frac{P_I + P_Q}{P_T}$$

$$C_I(t)^2 = C_Q(t)^2 = D_I(t)^2 = D_Q(t)^2 = 1$$

Conventional approaches to multiplexing additional signals with an existing I/Q quadrature modulation involve adding a third signal to one of the two I or Q phases. Unfortunately, this gives rise to the undesirable non-constant envelope characteristic. A signal can be linearly added to the I phase of the baseband waveform modulated onto the same carrier as the existing I/Q signals. For this case, the magnitude envelope of the signal  $A_0(t)$  is no longer constant due to presence of the time-varying component of  $A(t)$  in addition to the constant component of  $A_0(t)$ . This result is undesirable because the amplitude variations will give rise to amplitude modulation to amplitude modulation (AM-to-AM), and amplitude modulation to phase modulation (AM-to-PH) distortions when the signal is passed through a nonlinear amplifier. These and other disadvantages are solved or reduced using the invention.

## Summary of the Invention

An object of the invention is to provide a constant envelope composite signal with added subcarrier signals that do not distort existing signals when the composite signal is passed through a high-power amplifier operating near saturation.

Another object of the invention to provide for the modulation of new signals onto a quadrature multiplexed communication channel while controlling the power balance between signals while maintaining a constant envelope.

Yet another object of the invention is control the spectral separation of quadrature multiplexed signals within the allocated band through the use of subcarrier frequencies, subcarrier codes rate, and a subcarrier modulation index.

Yet another object of the invention is to enable the modulation of an orthogonal pair of subcarrier signals on to the I and Q phases of a quadrature modulated carrier.

Another object of the invention is to transmit the new M-code signals using either separate or combined-apertures with reduced distortion and losses.

A further object of the invention is to provide control of the distribution of energy among signals inside and outside an allocated band.

1        Yet a further object of the invention is to utilize cross-  
2        product intermodulation signals as useful communication signals.  
3

4        In a general aspect of the invention, quadrature product  
5        subcarrier modulation (QPSM) enables the transmission of a  
6        quadrature multiplexed carrier modulation with one or more  
7        subcarrier signals in the same constant-envelope waveform. The  
8        generalized QPSM enables the application of subcarrier modulation  
9        to quadrature multiplexed communication systems such as  
10      quadrature phase shift keying (QPSK) or minimum shift keying  
11      (MSK). The QPSM can be applied to both direct and  
12      spread-spectrum quadrature multiplexed communication systems. In  
13      particular, QPSM is advantageous for any spread spectrum system  
14      desiring additional spread signals with spectral isolation  
15      between new and existing pseudo random noise (PRN) code signals  
16      using the same transmitter power amplifier. QPSM can augment  
17      existing two-code spread-spectrum systems, without the need to  
18      employ time multiplexing or majority voting that result in  
19      significant power losses, while maintaining a constant envelope  
20      signal with spectral separation between existing signals and new  
21      signals with high efficiency. The QPSM enables a quadrature-  
22      multiplexed subcarrier spread-spectrum waveform modulation using,  
23      in general, multiple rate product codes that cause minimal  
24      interference to existing codes and the new codes. The modulation  
25      index can be used to control the distribution of energy between  
26      carrier and subcarrier signals.

27  
28

1       In a particular aspect of the invention, coherent adaptive  
2 subcarrier modulation (CASM) is provided as a flexible, efficient  
3 GPS modulation approach that can be tailored to different  
4 civilian and military GPS modes of operation to provide high  
5 efficiency without altering the basic modulation architecture.  
6 This efficiency can be tailored using a suitable modulation  
7 index, spreading code and subcarrier rates. CASM offers a  
8 constant envelope subcarrier modulation method particularly  
9 suitable the GPS. CASM provides a high efficiency of greater  
10 than 90% with inherent flexibility to fine tune the modulation  
11 architecture and maintain an ability to provide backward  
12 compatibility with current GPS signals within the allocated 24.0  
13 MHz GPS band. CASM can generate new GPS acquisition and tracking  
14 codes from products of the current GPS ranging signals and a  
15 newly defined subcarrier code and code partition function. CASM  
16 can generate a military GPS acquisition and a military GPS  
17 tracking signal from a single new code.

18

19       CASM is applicable to the transmission of quadrature  
20 duplexed military acquisition (MA) and military tracking (MT)  
21 signals in a flexible and efficient manner. The high efficiency  
22 approach is applied to both combined-aperture, with C/A, P(Y), MA  
23 and MT passed through the same upconverter amplifier chain and  
24 antenna and separate-aperture, with MA and MT signals transmitted  
25 out of a separate upconverter, amplifier chain and antenna from  
26 C/A and P(Y)) communication path. The CASM waveform is a highly  
27 efficient means of quadrature multiplexing new GPS military  
28 acquisition and tracking signals with flexibility in adjusting

1 the relative power of combined signals without greatly altering  
2 the power efficiency of the GPS waveform. The combined-aperture  
3 CASM offer power-efficient constant-envelope GPS modernization  
4 waveforms including the combination of C/A, P and M-code signals.  
5 The generated M-code signals are mathematically equivalent to the  
6 spatially combined signals.

7

8       CASM employs a subcarrier to phase modulated new M-code  
9 signals on the same carrier as the current C/A and P(Y) ranging  
10 codes. The constant-envelope CASM modulation is an evolution of  
11 the constant-envelope subcarrier modulation used on SGLS and  
12 other terrestrial and space systems to quadrature-multiplexed  
13 systems. Unlike prior subcarrier modulation developments, the  
14 CASM utilizes cross-product intermodulation terms as new ranging  
15 communication signals. In the present invention, using  
16 subcarrier modulation, cross product terms are interpreted as  
17 signals and not as losses. Preferably, the M-Code signals are  
18 generated by employing square-wave subcarriers to modulate the  
19 new military ranging signals, due to ease of hardware  
20 implementation, but CASM may be generated using both squarewave  
21 and sinewave subcarriers for GPS modernization. These and other  
22 advantages will become more apparent from the following detailed  
23 description of the preferred embodiment.

24  
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26  
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#### Brief Description of the Drawings

Figure 1 is a block diagram of a digital baseband phase modulator subcarrier modulation implementation of quadrature product subcarrier transmitter that can be used for generating general quadrature product subcarrier modulation (QPSM) signals as well as particular coherent adaptive subcarrier modulation (CASM) signals.

Figure 2 is a QPSM spectral plot.

Figure 3 is a CASM spectral plot.

## Detailed Description of the Preferred Embodiment

A detailed description of the preferred embodiment is described with reference to the figures using reference designations as shown in the figures. Referring to Figure 1, a quadrature product subcarrier modulation (QPSM) transmitter is used for transmitting in-phase code  $C_I$ , inphase data  $D_I$ , quadrature code  $C_Q$ , quadrature data  $D_Q$ , subcarrier code  $C_s$  and subcarrier data  $D_s$  signals originating from a code and data generator 10. The in-phase code and data signals are mixed by mixer 12, NRZ formatted by formatter 14, and power scaled by power factor 16 using mixer 18 providing the in-phase signal  $I_0$ . The quadrature code and data signals are mixed by mixer 20, NRZ formatted by formatter 22, and power scaled by power factor 24

1 using mixer 26 providing a quadrature signal  $Q_0$ . The mixers 12,  
2 18, 20, 26, power factors 16 and 24, and formatters 14 and 22 may  
3 be integrated as a Q/I phase processor module.

4

5 In-phase and quadrature data signals  $D_I$  and  $D_Q$  are received  
6 by a data partition function generator 28 providing a data  
7 partition signal  $\alpha$ . In-phase and quadrature code signals  $C_I$  and  
8  $C_Q$  are received by a code partition function generator 30  
9 providing a code partition signal  $\beta$ . The code partition signal  $\beta$   
10 is mixed by modulo two mixer 32 with the subcarrier code signal  
11  $C_s$  providing a mixed code signal communicated to another modulo  
12 two mixer 34 connected to another NRZ formatter 36. The data  
13 partition signal  $\alpha$  is also mixed by modulo two mixer 38 with the  
14 subcarrier data signal  $D_s$  providing a mixed data signal  
15 communicated to the modulo two mixer 34 providing a composite  
16 digital modulated signal to the formatter 36 that provides an  
17 encoded subcarrier modulation signal to the mixer 48.

18

19 A frequency synthesizer 40 is used to generate necessary  
20 clock signals for the generator 10. The synthesizer 40 also  
21 generates a subcarrier clock signal communicated to a digital  
22 subcarrier generator 42 for providing a digital subcarrier signal  
23 that is scaled by a scaler 46 using a modulation index  $m$  44 to  
24 provide a scaled digital subcarrier signal communicated to a  
25 mixer 48 that mixes the scaled digital subcarrier signal with the  
26 encoded subcarrier modulation signal from the formatter 36 to  
27 providing a modulated subcarrier signal communicated to a sine  
28 cosine processor 50 providing a sine subcarrier signal  $SS$  and a

1 cosine subcarrier signal CS. The generators 28, 30, 42,  
2 formatter 36, processor 50, scaler 46, and mixers 32, 34, 38, and  
3 48 may be integrated as a subcarrier digital baseband processor  
4 module.

5

6 The cosine subcarrier signal CS is communicated to mixers 52  
7 and 54 respectively receiving the  $I_0$  signal and  $Q_0$  signal and  
8 respectively providing a cosine  $I_0$  product signal and a cosine  $Q_0$   
9 product signal. The sine subcarrier signal SS is communicated to  
10 mixer 56 and 58 respectively receiving the  $I_0$  signal and  $Q_0$  signal  
11 and respectively providing a sine  $I_0$  product signal and a sine  $Q_0$   
12 product signal. The cosine  $I_0$  product signal from mixer 52 and  
13 the sine  $Q_0$  product signal from mixer 58 are subtracted by  
14 subtractor 60 providing a digital rotated I signal. The cosine  $Q_0$   
15 product signal and the sine  $I_0$  signal are added by an adder 62  
16 providing a digital rotated Q signal. The digital rotated I  
17 signal from the subtracter 60 is communicated to an in-phase  
18 digital-to-analog converter (IDAC) 64 providing an analog rotated  
19 I signal. The digital rotated Q signal from the adder 62 is  
20 communicated to a quadrature digital-to-analog converter (QDAC)  
21 66 providing an analog rotated Q signal.

22

23 The analog rotated I signal from IDAC 64 and the analog  
24 rotated Q signal from the QDAC 66 are received by a conventional  
25 quadrature modulator 68 providing an intermediate frequency (IF)  
26 modulated signal by quadrature modulation using an IF local  
27 oscillator signal IFLO from the frequency synthesizer 40. The IF  
28 modulated signal from quadrature modulator 68 is modulated by a

radio frequency (RF) local oscillator signal (RFLO) using a mixer 70 that provides an RF modulated signal communicated to a high power amplifier 72 that, in turn, provides an amplified RF modulated signal to a band pass filter 74 that, in turn, provides a filtered RF modulated signal to a transmitting antenna 76 for broadcast communication of a composite signal  $S(t)$ . The RF modulated signal from mixer 70 is expressed by the  $S_0(t)Q/I$  equation,  $S_0(t)$  and  $P_{TF}$  equations when the modulation index  $m$  is equal to zero. The gain of the high power amplifier is expressed as the square root of the total power  $P_T$ . The communication channel including the modulator 68, mixer 70, high power amplifier 72, channel band pass filter 74 and antenna 76 are conventional means well known in the art.

The new QPSM transmitter includes the addition of the subcarrier frequency generator 42 in the subcarrier digital baseband processor module and the scaler 44 to phase modulate the digital subcarrier. The mathematical equivalent of a phase rotation is constructed in the baseband by operating on the unrotated  $I_0$  and  $Q_0$  signals. This is achieved by transforming  $I_0$  and  $Q_0$  to  $I(t)$  and  $Q(t)$ . This complex-baseband approach can be implemented digitally in an application specific integrated circuit as a flexible means of subcarrier generation using the subcarrier processor 50.

The preferred transmitter shown in Figure 1 can be implemented in whole or in part using equivalent analog means. For example, the phase modulation may also be performed on the

1 subcarrier directly subject to the frequency limitations of an  
2 equivalent analog phase modulator. In this equivalent analog  
3 implementation, the encoded subcarrier modulation signal is  
4 directly phase modulated onto the RF carrier RFLO by applying the  
5 encoded subcarrier modulation signal to the input of an analog  
6 phase modulator, not shown, having a modulation index  $n$  that  
7 phase modulates the RFLO signal. In this equivalent analog phase  
8 modulator case, the sine and cosine subcarrier processor module  
9 and mixers 52, 54, 56, 58, as well as subtractor 60 and adder 62  
10 are bypassed and the  $I_0$  signal and  $Q_0$  signals are inputs directly  
11 into the quadrature modulator 68 connected directly to the high  
12 power amplifier 72.

13  
14       In a single subcarrier QPSM, the phase  $\phi(t)$ , is augmented by  
15 the subcarrier signal,  $\theta(t)$  modulated subcarrier signal from the  
16 mixer 48.

17  
18        $e(t) = m\phi_s(t) = mD_s(t)\alpha_D(t)c_s(t)\beta_C(t)\phi_s(t)$

19  
20  
21       The term  $\phi_s(t)$  is a periodic subcarrier signal that may be  
22 an arbitrary periodic waveform such as sine-wave, square-wave,  
23 triangle-wave, having an angular frequency  $\omega_s = 2\pi f_s$ , in rad/sec.  
24 The term  $m$  is the modulation index in radians.  $D_s(t)$  is the  
25 subcarrier data.  $c_s(t)$  is a non-return-to-zero (NRZ)-encoded PRN  
26 code with chipping rate  $R_{cs}$ . The term  $\phi_s(t)$  represents the  
27 composite subcarrier signal for the case of a single subcarrier.  
28  $\alpha_D(t)$  and  $\beta_C(t)$  are a function of the type of QPSM modulation

1 employed. These functions are typically binary functions and are  
2 used to preform the appropriate binary signals so that the  
3 desired resultant subcarrier code and data modulations will  
4 result in the composite spectrum. Using these definitions for  
5 forming  $I_0(t)$  and  $Q_0(t)$ , the QPSM waveform is defined as  $S(t)$ .  
6  $S(t)$  represents the phase modulation of  $s_0(t)$  by  $\theta(t)$ , and can be  
7 expressed by  $I(t)$  in-phase and  $Q(t)$  quadrature components out of  
8 the RF mixer 70.

9

$$10 \quad s(t) = I_0(t) \cos(\omega_c t + m\phi_s(t)) - Q_0(t) \sin(\omega_c t + m\phi_s(t))$$

11

12

13       The  $S(t)$  subcarrier modulated  $S(t)$  RF signal from mixer 70  
14 can be written in an expanded form.  
15

16

$$17 \quad s(t) = \left\{ \begin{array}{l} I_0(t) \cos(m\phi_s(t)) \\ -Q_0(t) \sin(m\phi_s(t)) \end{array} \right\} \cos(\omega_c t)$$

18       -      $\left\{ \begin{array}{l} Q_0(t) \cos(m\phi_s(t)) \\ +I_0(t) \sin(m\phi_s(t)) \end{array} \right\} \sin(\omega_c t)$ 

19       =      $I(t) \cos(\omega_c t) - Q(t) \sin(\omega_c t).$   
20

21

22       The analog  $I(t)$  and  $Q(t)$  signal, respectively from IDAC 64  
23 and QDAC 66 are subcarrier rotated signals expressed as  
24 subcarrier rotated carrier modulations,  $I_0(t)$  and  $Q_0(t)$ , as a  
25 function of subcarrier phase  $\phi(t)$ .  
26

27

28

1            $I(t) = I_0(t) \cos(m\phi_s(t)) - Q_0(t) \sin(m\phi_s(t))$

2            $Q(t) = Q_0(t) \cos(m\phi_s(t)) + I_0(t) \sin(m\phi_s(t))$

5           The envelope  $A(t)$  of the subcarrier augmented waveform is  
6           constant as the square root of the two times the sum of in-phase  
7           power  $P_I$  plus the quadrature power  $P_Q$ . Because the subcarrier  
8           modulation  $\theta(t) = m\phi_s(t)$  is a phase modulation equivalent to  
9           rotation of both  $I_0$  and  $Q_0$  components of  $S_0(t)$ , the constant  
10          envelope is maintained independent of the choice of  $\theta(t)$ . Hence,  
11          the total average power envelope of the subcarrier augmented  
12          waveform remains constant and is the sum of the in-phase power  $P_I$   
13          and the quadrature power,  $P_Q$ .

14

15          A single sinewave subcarrier can be an efficient means to  
16          modulate three signals in a constant-envelope waveform. For this  
17          case,  $\phi_s = \sin(\omega_s t)$ , so that  $m\phi_s$  is a function of  $\sin(\omega_s t)$ .

18

19           $m\phi_s = mD_s(t) \alpha_D(t) C_s(t) \beta_C(t) \sin(\omega_s t)$ .

20

21

22          The  $\cos(m\phi_s(t))$  and  $\sin(m\phi_s(t))$  terms may be expanded in  
23          terms of Bessel functions. The sinewave  $S(t)$  equation is a good  
24          approximate to terms of order  $J_2$ .

$$\begin{aligned}
 s(t) \cong & \left\{ \sqrt{2P_I} \cdot J_0(m) D_I(t) C_I - \right. \\
 & \left. \sqrt{2P_Q} \cdot 2J_1(m) D_Q(t) C_Q(t) \alpha_d(t) d_s(t) \beta_c(t) C_s(t) \sin(\omega_s t) \right\} \cos(\omega_c t) \\
 - & \left\{ \sqrt{2P_Q} \cdot J_0(m) D_Q(t) C_Q(t) + \right. \\
 & \left. \sqrt{2P_I} \cdot 2J_1(m) D_I(t) C_I(t) \alpha_d(t) d_s(t) \beta_c(t) C_s(t) \sin(\omega_s t) \right\} \sin(\omega_c t) \\
 & + \sqrt{2P_I} \cdot 2J_2(m) D_I(t) C_I(t) \cos(2\omega_s t) \cos(\omega_c t) \\
 & - \sqrt{2P_Q} \cdot 2J_2(m) D_Q(t) C_Q(t) \cos(2\omega_s t) \sin(\omega_c t).
 \end{aligned}$$

In the sinewave subcarrier QPSM approach, it is convenient to assume that the modulation index of the subcarrier waveform,  $m$  is less than  $\pi/2$  rads. For this case, the power contained in the  $J_2$  terms is much less than the power contained in  $J_1$  and  $J_0$  terms, for example, for  $M = 1$  rad the power of  $J_2$  term is less than 10db below the  $J_1$  and  $J_0$  terms. Furthermore, because these terms are spectrally separated from the carrier and subcarrier terms, the  $J_1$  and  $J_0$  terms will have a negligible contribution to the baseband correlations with  $C_I(t)$  and  $C_Q(t)$ . Thus, neglecting the  $J_2$  terms and applying the identities equations yields good approximation of the power content of  $S(t)$  for a sinewave subcarrier QPSM.

The term  $\alpha_D(t)$  is defined as the data partition function with  $[\alpha_D(t)]^2=1$ . The term  $\beta_C(t)$  is defined as the code partition function with  $[\beta_C(t)]^2=1$ . Both  $\alpha_D$  and  $\beta_C$  are defined in terms of QPSM variations. Both data and code QPSM messages have several variations. For  $\alpha_D(t) = D(t) = D_I(t) = D_Q(t)$ , the modulation is defined as doubly balanced QPSM because  $D(t)$  is balanced on both carrier channels and  $D_I(t) = D_Q(t) = D_s(t)$  is balanced on both subcarrier channels. In this case, the data modulation may be obtained by first tracking the carrier or the subcarrier signals. For  $\alpha_D(t) = D_s(t)$ , and  $D_I(t) = D_Q(t) = D(t)$ , the modulation is

defined as singly balanced QPSM because  $D(t)$  is balanced on both carrier channels and the data modulation on the subcarrier signals is identical to that on the carrier signals. In this case, the data modulation may be obtained by first tracking the carrier or the subcarrier signals. For  $\alpha_D(t) = D_s(t)$  and  $D_I(t) \neq D_Q(t)$ , the modulation is defined as, singly unbalanced QPSM because  $D(t)$  is balanced on both carrier channels and the data modulation on the subcarrier signals is identical to that on the carrier signals. In this case, the data modulation may also be obtained by first tracking the carrier or the subcarrier signals. For  $\alpha_D(t) = 1$ , with  $D_I(t)$ ,  $D_Q(t)$ , specified as different data messages, the modulation is defined as unbalanced QPSM because the data modulations on the in-phase and quadrature channels are different. For this case, the  $D_I(t)$ ,  $D_Q(t)$  messages must be demodulated prior to the demodulation of the  $D_s(t)$  subcarrier message. For  $\beta_c(t)=1$ , the resulting code is defined as normal QPSM. In this case, the carrier and subcarrier codes are selected so that the product is a higher order code. For example, the subcarrier code may be selected as a member of a preferred pair of M-sequences so that the resultant carrier-subcarrier product code is a gold code. For  $\beta_c(t) = C_I(t)C_Q(t)$ , the resulting code is defined as quadrature reversed QPSM. For  $\beta_c(t)=C_s(t)$ , the resulting code is defined as dual code QPSM. In general  $\beta_c(t)$  may take on any combination of codes or functional forms to tailor the code shape and energy distribution of the QPSM waveform. Combinations of code and data variations are designated by first data designation followed by code designation followed by QPSM. For example, a combination of

1       $\alpha_D(t) = D_s(t)$  and  $D_I(t) \neq D_Q(t)$  and  $\beta_C(t) = C_I(t)C_Q(t)$  would be known as  
2      singly unbalanced, quadrature reversed QPSM.

3

4      The QPSM waveform may also be developed for the squarewave  
5      subcarrier by setting  $\phi_s(t) = \text{Sqr}(\omega_s t)$ . For this case,  $\text{Cos}(m\phi_s t) =$   
6       $\text{Cos}(m)$  and  $\text{Sin}(m\phi_s t) = \text{Sin}(m)\phi_s(t)$ . After applying these  
7      definitions, the QPSM  $S(t)$  waveform for the square-wave  
8      subcarrier may then be expressed.

9

10     
$$S(t) = \sqrt{2P_I} \cdot \text{Cos}(m) D_I(t) C_I(t) \text{Cos}(\omega_c t)$$

11

12     
$$- \sqrt{2P_Q} \cdot \text{Cos}(m) D_Q(t) C_Q(t) \text{Sin}(\omega_c t)$$

13

14     
$$- \sqrt{2P_{QS}} \cdot \text{Sin}(m) D_{QS}(t) C_{QS}(t) \text{Sqr}(\omega_s t) \text{Cos}(\omega_c t)$$

15

16     
$$- \sqrt{2P_I} \cdot \text{Sin}(m) D_{IS}(t) C_{IS}(t) \text{Sqr}(\omega_s t) \text{Sin}(\omega_c t)$$

17

18

19      By appropriate choice of the modulation index  $m$  for sinewave  
20      QPSM, most of the usable power in the subcarrier waveform is  
21      transmitted to the signals,  $C_I$ ,  $C_Q$ ,  $C_{IS}$  and  $C_{QS}$ . The total power of  
22       $S(t)$  is expressed in terms of the total power of each component  $P_I$   
23      and  $P_Q$  for each  $J_0$ ,  $J_1$ , and  $J_2$  harmonics. The wasted power in the  
24      higher order harmonics of  $S(t)$  is unused and constitutes a signal  
25      loss. The power efficiency of the subcarrier waveform is then  
26      given by dividing the received power of the  $J_0$  carrier and  $J_1$   
27      subcarrier harmonics by the total power of  $P_T = P_I + P_Q$ , and  
28      expressed by a sinewave power efficiency equation.

$$\eta_P(m) = \frac{P_I * J_0^2(m) + P_Q * J_0^2(m) + P_I * 2J_1^2(m) + P_Q * 2J_1^2(m)}{P_I + P_Q} = J_0^2(m) + 2J_1^2(m)$$

The powers delivered to the carrier  $P_c = P_T J_0^2(m)$  component and subcarrier first harmonic  $P_s = P_T 2J_1^2(m)$  component can be compared. To select roughly equal power distribution between all four I and Q carriers, and I and Q subcarrier components, a modulation index of  $m=1.16$  with  $P_I = P_Q$  is selected. In this case, the efficiency of the sinewave subcarrier modulation approaches 95%. The power efficiency of the QPSM waveform treats the second and higher order subcarrier components as harmonic losses. For most applications, these components are outside the band of interest and/or carry too little energy to be detected. The QPSM waveform is over 95% power efficient, that is, only a 0.2 dB power loss, for modulation indices less than 1.16 for  $P_c$  less than or equal to  $P_{sc}$ . For values of  $m$  less than 1.2, the efficiency is over 95%. This efficiency, combined with QPSM constant-envelope makes the QPSM an effective modulation approach to augment existing quadrature-multiplexed communication systems or multiplex, spectrally separated communication channels about the same carrier.

For the case of a squarewave subcarrier, the total power of  $s(t)$  may be expressed as a function of the  $P_I$  and  $P_Q$  components. When both  $I_s$  and  $Q_s$  subcarrier signals are tracked in the QPSM, the efficiency of the QPSM waveform is 100% for all  $m$ , assuming

negligible band-limiting losses. This is illustrated by the following squarewave power efficiency equation.

$$\eta_p(m) = \frac{P_I \cdot \cos^2(m) + P_Q \cdot \cos^2(m) + P_I \cdot \sin^2(m) + P_Q \cdot \sin^2(m)}{P_I + P_Q} = 1$$

In reality, however, only signals modulated to the first harmonic of the squarewave subcarrier are contained in the band of interest, with the bandwidth of the subcarrier signals being several times less than the subcarrier frequency. Band limiting effects can be approximated by employing the Fourier expansion of the squarewave signal to order  $n=2k-1$ , to obtain the approximate result for a band-limited channel. The power in the subcarrier is proportional to the RMS value of  $\text{Sqr}(\omega_s t)$ . A typical approximation made be realized for squarewave subcarriers with neglected overlap between respective code and data signals at squarewave harmonics in band-limited channels for a squarewave subcarrier modulated QPSM. The power efficiency of the square-wave subcarrier QPSM with the modulation index corresponding to equal carrier and subcarrier power is  $m = 0.84$  and yields a power efficiency of 89% expressed by an approximate squarewave power efficiency equation.

$$\eta_p(m) \approx \cos^2(m) + \left(\frac{8}{\pi^2}\right) \sin^2(m)$$

1       Under realistic constraints of a band-limited channel, the  
2 squarewave subcarrier is generally less power efficient than the  
3 sinewave subcarrier.

4

5       Referring to Figure 2, a representative example of the QPSM  
6 modulation is shown by the power spectral density (PSD) of a  
7 singly-balanced QPSM presented for the case of a  
8 quadrature-multiplexed direct sequence spread-spectrum system  
9 with  $C_I$  selected as a 2.0 MHz PRN code,  $C_Q$  selected as a 1.0 MHz  
10 PRN code and  $C_s$  selected as a 4.0 MHz PRN code. In this example,  
11 the data modulation rates are selected at 10.0 KBPS so that the  
12 dominant spectral features would be the subcarrier modulated  $I_0$   
13 and  $Q_0$  PRN codes. The subcarrier was selected as a 12.0 MHz  
14 sinewave.

15

16       The generalized quadrature product subcarrier modulation  
17 applies subcarrier modulation to quadrature-multiplexed  
18 communication systems without the need to employ non-constant  
19 envelope modulation subject to amplitude modulation to amplitude  
20 modulation, and amplitude modulation to phase modulation  
21 distortions through a nonlinear high power amplifier. The  
22 spectral components reveal improved power distribution and power  
23 efficiency for both the square-wave and sinewave subcarriers.  
24 The power efficiency is approximately over 95% efficient for  
25 sinewave subcarriers and over 90% efficient for square-wave  
26 subcarriers for the case of equal carrier and subcarrier powers  
27 in band-limited channels.

28

1       The resultant waveforms are for a single subcarrier,  
2 however, QPSM can be applied to multiple subcarrier signals.  
3 Employing multiple rates in the general case, product codes can  
4 produce the desired spectral components in the resultant waveform  
5 and these signals are generalized by defining the multiple  
6 subcarrier phase modulation. In a generalized QPSM, a composite  
7 baseband signal of n-subcarriers is formed by replacing  $m\phi_s$  in  
8 the original approach with the composite signal. The subcarrier  
9 can be a single sinewave with  $\theta(t) = \sin(\omega_s t)$  or a squarewave with  
10  $\theta(t) = \text{Sqr}(\omega t)$ , or other periodic functions.  $\theta(t)$  is substituted  
11 into the subcarrier modulation equation  $m\phi_s$ , to generate a  
12 generalized subcarrier equation.

$$13 \quad \Theta(t) = \sum m^K D_s^K(t) \alpha_s^K(t) C_s^K(t) \beta_s^K(t) \Phi^K(t)$$

15       The term  $m^K$  is the modulation index of the K-th subcarrier.  
16 In the generalized form of the invention,  $\theta_K(t)$  is the K-th  
17 subcarrier and may be any periodic function having radian  
18 frequency,  $\omega_s^K = 2\pi s^K$ .  $D_s^K$  is K-th data sequence of the K-th  
19 subcarrier.  $\alpha_d^K(t)$  is the data partition function of the K-th  
20 subcarrier and  $\beta_c^K(t)$  is the code partition function of the K-th  
21 subcarrier. These partition functions, generally need not be  
22 binary.

24       QPSM employs the code and data partition functions to form  
25 desired subcarrier harmonics that are used to transmit  
26 information. Hence, cross-product terms are used as new  
27 communication signals. That is, the QPSM pre-multiplies the  
28

1 spread-data waveform by another spread data waveform so that the  
2 resultant product, naturally arising from the subcarrier  
3 modulation, is usable as a new communication signal. By doing  
4 so, the majority of the signals in the waveforms are designed for  
5 use as usable signals rather than allocated to wasted energy of  
6 intermodulation products. By pre-multiplying by code and data  
7 partition functions, QPSM allows for the implementation of  
8 subcarrier modulation on quadrature multiplexed communication  
9 signals. QPSM applies generally to any quadrature waveform  
10 including spread-spectrum waveforms. For the general case,  
11 neither the data nor the code partition functions must be binary.  
12 The functions need only to be selected such that the  
13 cross-product terms in the resultant subcarrier modulation are  
14 designed to be the signal of interest.

15

16 A specific example of the general QPSM to quadrature spread  
17 spectrum communication waveforms is coherent adaptive subcarrier  
18 modulation (CASM). CASM allows for the presence of two  
19 time-varying quadrature multiplexed carrier signals in addition  
20 to the subcarrier signals that modulate the phase of the carrier,  
21 that are modulated producing a constant envelope composite signal  
22 using a single modulation index. The ability to employ  
23 subcarrier phase modulation to a quadrature-modulated signal is  
24 facilitated by the unique formulation of the CASM. CASM can be  
25 applied to GPS waveforms utilizing quadrature multiplexing and  
26 subcarrier modulation to transmit at least three GPS ranging  
27 signals in the same constant-envelope waveform. The specific  
28 formulation of the CASM is generalized to multiple civilian and

1 military GPS signals that may be on any combination of the  $I_0(t)$   
2 carrier,  $Q_0(t)$  carrier and subcarrier signals. The formatting of  
3 these signals is not a limitation of CASM and the partition  
4 functions  $\alpha_D^K(t)$  and  $\beta_C^K(t)$  defined for the i-th subcarrier, and  
5 may be composed from any combination of NRZ spreading codes,  
6 other periodic function at any frequency, and the current GPS  
7 data modulation commonly known as the GPS navigation message,  
8 and/or spreading codes including the GPS C/A code, and P/Y code.  
9 The specific CASM is selected to optimize the signals of interest  
10 and to suppress interference between signals in the composite  
11 waveform. Hence, the QPSM is not limited to sinewave subcarriers  
12 but may be generalized to an arbitrary number of square-wave, or  
13 other periodic, subcarrier signals. The CASM describes a  
14 specific methodology for use of multiple code and data partition  
15 functions to form an inherently constant-envelope waveform from  
16 products of carrier signals, code and data partition functions,  
17 and one or more subcarrier signals selected to optimize the  
18 signals of interest and suppress interference between signals.

19

20 CASM is applied to the modulation of coherently related  
21 quadrature duplexed military acquisition (MA) and military  
22 tracking (MT) signals onto quadrature phases of a subcarrier in  
23 constant envelope. CASM enables the modulation of new signals  
24 onto the quadrature multiplexed GPS C/A and P(Y) code signals.  
25 CASM pre-multiplies the subcarrier data and code modulation by  
26 the binary data and code partition functions,  $\alpha_D$  and  $\beta_C$  to enable  
27 the utilization of subcarrier intermodulation products that would  
28 otherwise be unusable signals. By so doing, the subcarrier

1 modulation results in a highly efficient waveform, with two  
2 aspects of the same signal that may be optimized for military  
3 acquisition MA and military tracking MT signals. The CASM  
4 approach is based on the more general quadrature product  
5 subcarrier modulation (QPSM) applicable to the augmentation of an  
6 existing quadrature multiplexed communication system with new  
7 communication signals.

8

9 In Figure 3, the power spectral density of the a  
10 quadrature-multiplexed spread-spectrum transmitter is shown. The  
11 transmitter uses a modulation index  $m=1.16$  rad for a QPSM  
12 waveform obtained for a complex-baseband implementation of the  
13 output of a QPSM transmitter. The carrier modulation curve can  
14 be thought of as a subset of the QPSM signals with  $m=0$ . The  
15 spectrum illustrates the spectral components of the QPSM waveform  
16 at  $\pm$  multiples of the 12.0 MHz subcarrier frequency. The  
17 position and magnitude of the QPSM harmonics reveal harmonic  
18 distribution and power content. In particular, the magnitude of  
19 the  $J_2$  harmonic of the carrier for  $m=1.16$  is less than 10.0 dB  
20 below that of the  $J_0$  carrier components.

21 For the GPS CASM applications,  $\alpha_D$  is equal to the GPS  
22 navigation data message and  $\beta_c(t)$  is equal to C/A or P/Y. In the  
23 exemplar form, sinewave or square-wave subcarriers may be used.  
24 For a sinewave subcarrier,  $\theta_s = \sin(\omega_s t)$ . For square-wave  
25 subcarriers, one can generate Manchester encoded PRN code signals  
26 by setting  $\theta_s(t) = \text{Sqr}(\omega_s t)$ , with the frequency of the squarewave  
27 subcarrier signal set equal to the frequency of the PRN code  
28 signal.

Using the equations for  $I_0(t)$  and  $Q_0(t)$ , the CASM phase-modulated GPS waveform is given by  $S(t)$  and represents the phase modulation of the current GPS waveform  $S_0(t)$ . CASM can be used to modulate a wide range of M-code signals, such as binary offset carrier variations, Manchester variations, or offset carrier variations. Also, the power ratio and code and data distribution for the I and/or Q channels, and nature of the M-code signal are easily controlled through the adjustment of  $m$ ,  $P_I$ ,  $P_Q$ , and the selection of the binary partition functions,  $\alpha_D$  and  $\beta_C$ . CASM is preferably applied to existing GPS waveforms through the use of an analog phase modulator or through complex baseband subcarrier phase rotations. For subcarrier frequencies less than or equal to roughly 10.23 MHz, the complex baseband approach is a more flexible alternative, well within present day technology limits.

CASM may be implemented using a rapid prototyping capability to convert the transmitter design into a gate level design and downloaded to a single XYLINX 4085XL field programmable gate array with approximately 40K gates. A ten bit sine and cosine lookup table size leads to a subcarrier phase noise, due to quantization, of approximately -60 dBc. This level is adequate to maintain the current signal quality level of the current GPS signal. Unlike hard-limiting or Majority-vote combining, the CASM approach is applicable to the constant-envelope modulation of both squarewave and sinewave modulated ranging signals. For a square-wave subcarrier, the lookup tables can be implemented in non-real-time using  $\text{Cos}(m\phi_s) = \text{Cos}(m)$  and  $\text{Sin}(m\phi_s(t)) =$

1       $\sin(m)\phi_s(t)$  identities for a binary subcarrier modulation phase  
2       $\phi_s$ .    Only the constant values  $\cos(m)$  and  $\sin(m)$  need to be  
3      evaluated for the squarewave CASM.

4

5      CASM can be used with a single sinewave subcarrier as a  
6      constant envelope multiple mode spread spectrum subcarrier  
7      modulation for GPS.   Considering only terms to order J2.   In  
8      general, there are an infinite number of carrier harmonics ( $J_0$ ,  
9       $J_2$ ,  $J_4$ , ...) and subcarrier harmonics ( $J_1$ ,  $J_3$ ,  $J_5$ ...) but only  
10     the first carrier and subcarrier harmonics need be considered for  
11      $m \leq \pi/2$ .   For this range of the modulation index, the sinewave  
12     CASM approach is over 95% power efficient.   For values of  $m$   
13     greater than  $\pi/w$ , a much greater fraction of the transmitter  
14     power is lost to the  $n=2, 3, 4, 5$  harmonics outside of the GPS  
15     band depending upon subcarrier selection.   The current GPS  
16     waveform is recovered by setting  $m=0$ .   The composite subcarrier  
17     PRN product codes and data messages can be expressed to a good  
18     approximation by only the dominant terms in the harmonic  
19     expansion by applying the sinewave subcarrier expression with the  
20     use of some well-known Bessel function identities.   By the  
21     selection of  $\alpha_D(t)$  and  $\beta_D(t)$ ,  $C_{IS}$  and  $C_QS$  are coherently related to  
22     new military acquisition and tracking signals with the same  
23     M-code data modulation on both of these subcarrier signals.   With  
24     the current partitioning of subcarrier code and data, the new MA  
25     acquisition and MT tracking codes are derived from the single new  
26     military PRN code  $C_s(t)$ .   The P(Y)-code is a very long PRN code  
27     repeating each week.   The randomness properties of the P(Y) code  
28     are used by military GPS receivers.   By selecting the  $C_s$  code to

be a non-periodic tracking code, the correlation randomness properties of the MT code will be determined primarily by the properties of the  $C_s$  code. The appropriate selection of the  $C_s$  code relatively prime to the product of (C/A-code) \* (P(Y)-Code) will result in a code with a length that is equal to the product of the lengths of the  $C_s$  and the P(Y)-Codes, much longer than the current P(Y)-code. The generation of a long code from two relatively prime sequences is well known and is the primary basis for the current GPS P(Y)-code length. The M-code data modulation is determined by the current selection of data partition function, similar to the case of the PRN codes, by  $D_M(t) = D_{IS}(t) = D_{QS}(t) = D_s(t)$  where  $D_M(t)$  is defined as the new military navigation data message. The current selection of the data partition function leading to a single M-code data message, is convenient to adapt the CASM to the currently favored option of a single new M-code data modulation for the new military M-code signals but is not a limitation of the general approach. By setting  $\beta_c(t) = C_p(t)$  instead of the C/A code, the I/Q phasing of the MA and MT codes are reversed. For this case,  $C_{MA} = C_{IS}(t) = C_s(t)$  and  $C_{MT}(t) = C_{QS}(t) = C_s(t)C_{C/A}(t)C_p(t)$ . For this case, the partition of the data modulation remains unchanged and the MA and MT signals obtain power from alternate phases of the carrier, that is, the MA signal on the Q channel and MT signal on the I channel rather than the MA signal on I channel and the MT signal on the Q channel. The  $C_s(t)$  is defined as  $C_{MA}(t)$ . A single new subcarrier acquisition code  $C_s(t)$  is defined to generate both an acquisition and a tracking code signal. The designation acquisition and tracking does not mean that these signals cannot

both be acquired and tracked, analogous to the case of C/A and P(Y) codes, but only that these signals are optimized for the these GPS operating states. The efficient use of this code with CASM utilizes this code as a useful ranging signal in a well controlled manner. The power contained in the MA and MT signals can be combined using a dual-code correlator to utilize the total power in the MA and MT signals.

Due to the ease of digital implementation, square-wave modulated ranging codes have become popular for use as a new M-code signal. The resulting higher harmonics of the carrier are not present in the square-wave CASM approach. Thus, to raise the subcarrier power well above the carrier power, M is increased to a value near  $\pi/2$ . For this case, the only losses are due to the band-limiting effects inherent in any square-wave modulated ranging signal. The current GPS waveform can be recovered for the case of  $m=0$ .

The sinewave and square-wave CASM approaches may be generalized to an arbitrary number of subcarriers into the generalized modulation subcarrier equation. This method may be useful to enable multiple military and, perhaps, additional civilian ranging signals to be transmitted in a single constant envelope waveform. The notation CASM ( $r, n$ ) denotes the military acquisition (MA) and military tracking (MT) pair of signals generated by the CASM modulation method. The MA signal, MA ( $r, n$ ), is formed from the product of a  $n \times 1.023$  MCPS spreading code modulated by a  $r \times 1.023$  MHz subcarrier and the MT signal,

1 MT( $r, n$ ), is given by the MA signal modulated by C/A code and P(Y)  
2 code. In general, the MT code is given by the product of the MA  
3 code times an unencoded 10.23 MHz NRZ code. The MT-code signal  
4 will have a length greater than or equal to the current P(Y)-code  
5 signal, depending upon the selection of the MA code.

6

7 As an example of the CASM signals, a CASM(10,2) quadrature  
8 modulated pair of ranging signals consists of a MA(10,2)  
9 acquisition signal on the I phase of the carrier along with the  
10 P(Y) code and an MT(10,10) tracking signal on the Q phase along  
11 with the C/A Code that are modulated using the modulator depicted  
12 in Figure 1 with  $C_I$  equal to the P(Y) code,  $C_Q$  equal to the C/A  
13 code and  $C_s$  equal to a 2.046 MCPS NRZ formatted M-Code. In this  
14 example, the subcarrier signal is a 10.23 MHz squarewave,  $D_I$  is  
15 equal to  $D_Q$  that is also equal to the current GPS data navigation  
16 message and  $D_s$  is the new military GPS subcarrier data message.  
17 The data partition function,  $\alpha$  is equal to the current GPS  
18 navigation message and  $\beta$  is equal to the C/A code.

19

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21 The power spectral densities (PSD) of this example are  
22 compared to the composite P(Y) code and C/A code spectrum  
23 depicted in Figure 3 for the MA(10,2) and MT(10,10) signals  
24 respectively. With the exception of the P(Y)-code PSD, which was  
25 calculated analytically, the MA and MT code PSDs were determined  
26 from a simulation employing the exact C/A-codes and P(Y)-codes  
27 for PRN 1, and a 20'th order M-sequence for the MA Code. The  
28 PSD's were then obtained from a 1024 point Fast Fourier Transform

1 followed by a discrete time autocorrelation using 512 Lags and a  
2 Hanning window function. The sampling rate of the simulation was  
3  $1.2276 \times 10^8$  samples per second. The MA signal for this option  
4 consists of a 2.046 MHz PRN code ( $C_s(t)$ ) modulated by a 10.23 MHz  
5 squarewave subcarrier. The product of  $C_s(t)C_p(t)C_{C/A}(t)$  results in  
6 an unbalanced 10.23 MHz PRN Code. The product of this code with  
7 a squarewave modulated ranging signal results in a 10.23 MHz  
8 Manchester code.

9  
10 In general, it can be shown that the integer relation  
11 between the subcarrier frequency and the PRN code chip rate, as  
12 in the CASM(10,2) example, is not necessary for new M-code  
13 signals to have minimal interference with the C/A-code and P(Y)-  
14 code signals from a given satellite. Rather, it is only  
15 necessary that the frequency of the subcarrier, such as a  
16 sinewave or squarewave, is much greater than the GPS data rate.  
17 This is true for any subcarrier of frequency greater than 1.023  
18 MHz.

19  
20 The non-integer relationship has been simulated for the case  
21 of a CASM using a 5.115 MHz sinewave subcarrier modulating a  
22 4.092 MHz PRN code ( $C_s$ ). For this example, the simulated variance  
23 of the on-time C/A code correlated with the received Q-signal  
24 ( $C/A + MT$ ) and on-time P(Y)-code correlated with the received I-  
25 signal ( $P + MA$ ) was  $4.14e-05$  (with unit power in the PRN-codes).  
26 Relative to a signal level of -160 dBW, this value corresponds to  
27 a multiplexing noise density of only -203 dBW as compared to  
28

1 about -140 dB for thermal noise power out of a C/A-code  
2 correlator. This level is similar to the cross-correlation  
3 magnitude observed for the correlation of on-time C/A-code with a  
4 filtered 5.115 MHz Manchester code. This magnitude has been  
5 postulated to be identically zero if the bandwidth of the GPS  
6 system were infinite. This performance, together with CASM's  
7 inherent constant-envelope nature, make the approach a flexible,  
8 efficient modulation technique, capable of accommodating a wide  
9 range of signal modulation alternatives and providing the  
10 capability to control spectral isolation between signals inside  
11 and outside of the GPS band. Its flexibility minimizes the cost,  
12 complexity and risk associated with implementation of the GPS  
13 transmitter circuitry.

14

15 In the CASM waveform approach, both MA and MT code signals  
16 are generated from a single new ranging code. Each of these  
17 signals can be acquired and tracked independently of each other  
18 and independently of the C/A and P(Y) codes. Because the MA and  
19 MT ranging signals have low cross-correlation, as has been  
20 verified through simulation, and these signals are coherently  
21 related. The power of the MA and MT codes can be combined through  
22 the implementation of a non-coherent dual code correlator, not  
23 shown. The significant difference between the conventional  
24 correlator and the dual code correlator is that the sum of the MT  
25 and MA codes are used as local references rather than just the MA  
26 and MT codes alone. This straightforward implementation will  
27 result in the utilization of the total power contained in both  
28 the MA and MT signals during acquisition and tracking.

1       The CASM approach enables a highly efficient means to  
2 generate complementary military acquisition and tracking signals  
3 that are adaptable to both separate and combined-aperture  
4 implementations of the GPS modernization signals. In particular,  
5 the QPSM-based CASM modulator permits the constant envelope  
6 modulation of these new signals and existing GPS ranging signals  
7 to enable efficient transmission through a single high-power  
8 amplifier. Both sinewave and squarewave subcarrier  
9 implementations of CASM are straightforward complex-baseband  
10 implementation of a CASM modulator design. The general efficiency  
11 of the approach for both squarewave and sinewave subcarriers was  
12 demonstrated be in the range of 70% to 95% for practical  
13 subcarrier power ratios. Those skilled in the art can make  
14 enhancements, improvements and modifications to the invention,  
15 and these enhancements, improvements and modifications may  
16 nonetheless fall within the spirit and scope of the following  
17 claims.

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1 What is claimed is:

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3 1. A system for modulating DS data on an I phase communicating  
4 DI data and on a Q phase communicating DQ data, the I phase and Q  
5 phase are phases of a modulated carrier signal communicating the  
6 DI data and the DQ data and the DS data, the carrier signal has a  
7 total phase equal to arctangent of the Q phase divided by the I  
8 phase, the system comprising,

9       an encoder for encoding the DI data and the DQ data  
10 respectively into an Io encoded signal and a Qo encoded signal,

11       an encoded subcarrier modulation signal generator for  
12 receiving one or more of the DS data and the DI data and the DQ  
13 data and for generating an encoded subcarrier modulation signal,  
14 the encoded subcarrier modulation signal comprises a product of a  
15 data partition function and the DS data, the data partition  
16 function is a function of one or more of the DI data and the DQ  
17 data and the DS data,

18       a modulator for modulating a subcarrier signal by the  
19 encoded subcarrier modulation signal for providing a modulated  
20 subcarrier signal, for modulating the total phase of the carrier  
21 signal by the modulated subcarrier signal, for modulating the I  
22 phase of the carrier signal by the Io encoded signal and by an I  
23 phase subcarrier signal to provide an I phase carrier signal and  
24 for modulating the Q phase of the carrier signal by the Qo  
25 encoded signal and by a Q phase subcarrier signal to provide a Q  
26 phase carrier signal, the modulator combining the Q phase carrier  
27 signal and the I phase carrier signal as a composite signal, the  
28 I phase subcarrier signal is an I intermodulation product of the

1 encoded subcarrier modulation signal and the Qo encoded signal,  
2 the Q phase subcarrier signal is a Q intermodulation product of  
3 the encoded subcarrier modulation signal and the Io encoded  
4 signal, the ratio of the Q intermodulation product over the I  
5 intermodulation product is equal to the ratio of the Io encoded  
6 signal over the Qo encoded signal, the composite signal has a  
7 constant amplitude envelop.

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1       2. The system of claim 1, wherein  
2           the encoder comprises:  
3              a Q encoder for encoding the DQ data into the Qo encoded  
4 signal; and  
5              an I encoder for encoding the DI data into the Io encoded  
6 signal,  
7              the encoded subcarrier modulation signal generator  
8 comprises:  
9              a data partition function generator for receiving one or  
10          more of the DI data and the DQ data and the DS data and for  
11          generating a data partition signal;  
12          a modulo two mixer for mixing the data partition signal with  
13          the DS data into a modified DS data signal; and  
14          a data encoder encoding the modified DS data signal into the  
15          encoded subcarrier modulation signal,  
16          the modulator comprises:  
17              a subcarrier generator for generating the subcarrier signal;  
18              a multiplier for multiplying the subcarrier signal by a  
19          modulation index for generating a scaled subcarrier signal;  
20          a scaling mixer for mixing the scaled subcarrier signal with  
21          the encoded subcarrier modulation signal for providing the  
22          modulated subcarrier signal;  
23          a sine and cosine subcarrier processor for receiving the  
24          modulated subcarrier signal for generating a sine subcarrier  
25          signal and a cosine subcarrier signal, the sine subcarrier signal  
26          is modulated by the DS data, the cosine subcarrier signal is  
27          unmodulated by the DS data;  
28          a carrier phase rotator for combining the sine subcarrier

1 signal and the cosine subcarrier signal with both of Io encoded  
2 signal and the Qo encoded signal and for providing I and Q  
3 rotated signals, the I rotated signal comprises a scaled Io  
4 encoded signal for communicating the DI data and comprises a  
5 scaled I phase subcarrier signal for communicating the DS data,  
6 the Q rotated signal comprises a scaled Qo encoded signal for  
7 communicating the DQ data and a scaled Q phase subcarrier signal  
8 for communicating the DS data, the scaled I phase and Q phase  
9 subcarrier signals are the I and Q intermodulation products and  
10 are generated when the sine and cosine subcarrier signals are  
11 rotated and combined with Io encoded signal to form the I rotated  
12 signal and when the sine and cosine subcarrier signals are  
13 rotated and combined with the Qo encoded signal to form the Q  
14 rotated signal, the scaled I phase and scaled Q phase subcarrier  
15 signals are orthogonal and are the I and Q intermodulation  
16 products of the Io and Qo encoded signals modulated by harmonics  
17 of the modulated subcarrier signal, the I and Q rotated signals  
18 are scaled by harmonics of the scaled subcarrier signal;  
19 and,

20 a quadrature modulator for receiving the I and Q rotated  
21 signals and the carrier signal for respective I and Q phase  
22 modulation of the carrier signal by the I and Q rotated signals  
23 to provide the composite signal having the I phase and Q phase,  
24 the DI data is communicated on the I phase of the composite  
25 signal, the DQ data is communicated on the Q phase of the  
26 composite signal, and the DS data is communicated on both of the  
27 I phase and Q phase of the composite signal, the constant  
28 amplitude envelope results from the I and Q phase modulation of

1 the carrier signal by the modulated subcarrier signal.

2

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4 3. The system of claim 2, wherein the modulation index is less

5 than or equal to  $\pi/2$  radians.

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8 4. The system of claim 1 wherein

9 the encoder comprises:

10 a Q encoder for encoding the Q data into the Qo encoded

11 signal; and

12 an I encoder for encoding the I data into the Io encoded

13 signal,

14 the encoded subcarrier modulation signal generator

15 comprises:

16 a data partition function generator for receiving one or

17 more of the DI data and the DQ data and the DS data for

18 generating a data partition signal;

19 a modulo two mixer for mixing the data partition signal with

20 the DS data into a modified DS data signal; and

21 a data encoder encoding the modified DS data signal into the

22 encoded subcarrier modulation signal,

23 the modulator comprises:

24 a subcarrier generator for generating the subcarrier signal;

25 a subcarrier modulator for modulating the encoded subcarrier

26 modulation signal onto the subcarrier signal to provide the

27 modulated subcarrier signal;

28 a quadrature modulator for modulating Io encoded signal and

1 Q<sub>o</sub> encoded signal onto an IF signal for providing a quadrature IF  
2 signal;

3 a phase modulator having a modulation index for phase  
4 modulating an RF signal by the modulated subcarrier signal to  
5 provide a modulated subcarrier RF signal; and

6 a mixer for mixing the quadrature IF signal with the  
7 modulated subcarrier RF signal to provide the composite signal  
8 comprising the carrier signal that is a product of the IF signal  
9 and the RF signal.

10  
11 5. The system of claim 4, wherein the subcarrier signal is a  
12 sinewave signal.

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14  
15 6. The system of claim 1, wherein,  
16 the encoder is further for setting an I phase to Q phase  
17 power ratio of power of the I<sub>o</sub> encoded signal relative to power  
18 of the Q<sub>o</sub> encoded signal, and for further setting the same I  
19 phase to Q phase power ratio of power of the Q phase subcarrier  
20 signal relative to power of the I phase subcarrier signal, and  
21 the modulator is defined by a modulation index for setting a  
22 carrier to subcarrier power ratio between the power of I<sub>o</sub> and Q<sub>o</sub>  
23 encoded signals relative to the I phase and Q phase subcarrier  
24 signals.

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27 7. The system of claim 1, wherein the subcarrier signal is a  
28 periodic signal.

8. A system for modulating DS data on an I phase communicating  
DI data and on a Q phase communicating DQ data, the I phase and Q  
phase are phases of a modulated carrier signal communicating the  
DI data and DQ data, the carrier signal has a total phase equal  
to arctangent of the Q phase divided by the I phase, the DI data  
is communicated in spread spectrum signals spread by an CI code,  
the DQ data is communicated in spread spectrum signals spread by  
an CQ code, the DS data is communicated in spread spectrum  
signals spread by an CS code, the DS data is subcarrier data and  
CS code is a subcarrier code, the system comprising,

an encoder for encoding the DI data spread by the CI code  
into an Io encoded signal, and for encoding the DQ data spread by  
the CQ code into a Qo encoded signal,

an encoded subcarrier modulation signal generator for  
receiving the DS data and the CS code and the DI data and the CI  
code and the DQ data and the CQ code and for generating an  
encoded subcarrier modulation signal, the encoded subcarrier  
modulation signal comprises a product of a data partition  
function and a code partition function and the DS data and the CS  
code, the data partition function is a function of one or more of  
the DI data and the QI data and the DS data, the code partition  
function is a function of one or more of the CI code and the CQ  
code and the CS code, and

a modulator for modulating a subcarrier signal by the  
encoded subcarrier modulation signal for providing a modulated  
subcarrier signal, for modulating the total phase of the carrier  
signal by the modulated subcarrier signal, for modulating the I  
phase of the carrier signal by the Io encoded signal and by an I

1 phase subcarrier signal to provide an I phase carrier signal and  
2 for modulating the Q phase of the carrier signal by the Qo  
3 encoded signal and by an Q phase subcarrier signal to provide a Q  
4 phase carrier signal, the carrier modulator combining the Q phase  
5 carrier signal and the I phase carrier signal as a composite  
6 signal, the Q phase subcarrier signal is a Q intermodulation  
7 product of the encoded subcarrier modulation signal and the Io  
8 encoded signal, the I phase subcarrier signal is an I  
9 intermodulation product of the encoded subcarrier modulation  
10 signal and the Qo encoded signal, the ratio of the Q  
11 intermodulation product over the I intermodulation product is  
12 equal to the ratio of the Io encoded signal over the Qo encoded  
13 signal, the composite signal has a constant amplitude envelop.

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1       9. The system of claim 8, wherein,  
2                  the data partition function is an alpha function, the alpha  
3                  function has a square identity, the alpha function is selected  
4                  from a group consisting of a first alpha function equaling DI  
5                  that equals DQ, a second alpha function equaling DS when DI equal  
6                  to DQ, a third alpha function equaling DS when DI does not equal  
7                  DQ, a fourth alpha function equaling one when DI does not equal  
8                  DQ, and a fifth alpha function equaling one when DI equals DQ,  
9                  and

10                 the code partition function is a beta function, the beta  
11                 function has a square identity, the beta function is selected  
12                 from a group consisting of a first beta function equaling one, a  
13                 second beta function equaling CI times CQ, a third beta function  
14                 equaling CI, a fourth beta function equaling CQ, and a fifth beta  
15                 function equaling CS.

16  
17       10. The system of claim 8, wherein the encoder is further for  
18                 setting a power ratio of the I<sub>0</sub> encoded signal relative to Q<sub>0</sub>  
19                 encoded signals, and for setting the same power ratio of the Q  
20                 phase subcarrier signal relative to the I phase subcarrier  
21                 signal.

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23  
24       11. The system of claim 8, wherein the modulator is defined by a  
25                 modulation index for setting a power ratio between power of I<sub>0</sub>  
26                 and Q<sub>0</sub> encoded signals relative to power of the Q phase and I  
27                 phase subcarrier signals.

1       12. The system of claim 11, wherein power of the Q phase and I  
2       phase subcarrier signals is less than power of the Io and Qo  
3       encoded signals modulated on the carrier signal.

4

5       13. The system of claim 8, wherein the modulator comprises,  
6            a subcarrier generator for generating the subcarrier signal;  
7            a subcarrier modulator for modulating the encoded subcarrier  
8       modulation signal onto the subcarrier signal to provide a  
9       modulated subcarrier signal;  
10            a quadrature modulator for modulating Io encoded signal and  
11       Qo encoded signal onto an IF signal for providing a quadrature IF  
12       signal;  
13            a phase modulator having a modulation index for phase  
14       modulating an RF signal by the modulated subcarrier signal to  
15       provide a modulated subcarrier RF signal; and  
16            a mixer for mixing the quadrature IF signal with the  
17       modulated subcarrier RF signal to provide the composite signal  
18       comprising the carrier signal that is a product of the IF signal  
19       and the RF signal.

20

21       14. The system of claim 8, wherein the encoder comprises,  
22            a Q mixer for spreading the DQ data by the CQ code to  
23       provide a DCQ spread spectrum signal,  
24            a Q encoder for encoding the DCQ spread spectrum signal into  
25       the Qo encoded signal,  
26            a Q amplifier for setting a Q power level of the Qo encoded  
27       signal,  
28            an I mixer for spreading the DI data by the CI code to

1 provide a DCI spread spectrum signal,  
2       an I encoder for encoding the DCI spread spectrum signal  
3 into the Io encoded signal, and  
4       an I amplifier for setting an I power level of the Io  
5 encoded signal.

6

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8 15. The system of claim 14, wherein the I power level does not  
9 equal the Q power level.

10

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12 16. The system of claim 8, wherein the encoded subcarrier  
13 modulation signal generator comprises,  
14       a data partition function generator for receiving one or  
15 more of the DS data and the DI data and the DQ data and for  
16 generating a data partition signal,  
17       a code partition function generator for receiving one or  
18 more of the CS code and the CI code and the QI code and for  
19 generating a code partition signal,  
20       a data mixer for modulo two mixing the DS data and the data  
21 partition signal into a modulo two data signal,  
22       a code mixer for modulo two mixing the CS code and the code  
23 partition signal into a modulo two code signal,  
24       a modulo two mixer for modulo two mixing the modulo two data  
25 signal with the modulo two code signal for providing a modified  
26 subcarrier data signal, and  
27       a data encoder for encoding the modified subcarrier data  
28 signal into the encoded subcarrier modulation signal.

1       17. The system of claim 8, wherein the modulator comprises,  
2            a subcarrier generator for generating the subcarrier signal;  
3            a multiplier for multiplying the subcarrier signal by a  
4 modulation index for generating a scaled subcarrier signal;  
5            a scaling mixer for mixing the scaled subcarrier signal with  
6 the encoded subcarrier modulation signal for providing a  
7 modulated subcarrier signal;

8            a sine and cosine subcarrier processor for receiving the  
9 modulated subcarrier signal for generating a sine subcarrier  
10 signal and a cosine subcarrier signal, the sine subcarrier signal  
11 is modulated by the DS data, the cosine subcarrier signal is  
12 unmodulated by the DS data;

13          a carrier phase rotator for combining the sine subcarrier  
14 signal and the cosine subcarrier signal with both of Io encoded  
15 signal and the Qo encoded signal and for providing I and Q  
16 rotated signals, the I rotated signal comprises a scaled Io  
17 encoded signal for communicating the DI data and comprises a  
18 scaled I phase subcarrier signal for communicating the DS data,  
19 the Q rotated signal comprises a scaled Qo encoded signal for  
20 communicating the DQ data and a scaled Q phase subcarrier signal  
21 for communicating the DS data, the scaled I phase and Q phase  
22 subcarrier signals are the I and Q intermodulation products and  
23 are generated when the sine and cosine subcarrier signals are  
24 rotated and combined with Io encoded signal to form the I rotated  
25 signal and when the sine and cosine subcarrier signals are  
26 rotated and combined with the Qo encoded signal to form the Q  
27 rotated signal, the scaled I phase and scaled Q phase subcarrier  
28 signals are orthogonal and are the I and Q intermodulation

1 products of the  $I_o$  and  $Q_o$  encoded signals modulated by harmonics  
2 of the modulated subcarrier signal, the I and Q rotated signals  
3 are scaled by harmonics of the scaled subcarrier signal; and  
4 a quadrature modulator for receiving the I and Q rotated  
5 signals and the carrier signal for respective I and Q phase  
6 modulation of the carrier signal by the I and Q rotated signals  
7 to provide the composite signal having the I phase and Q phase,  
8 the DI data is communicated on the I phase of the composite  
9 signal, the DQ data is communicated on the Q phase of the  
10 composite signal, and the DS data is communicated on both of the  
11 I phase and Q phase of the composite signal, the constant  
12 amplitude envelope results from the I and Q phase modulation of  
13 the carrier signal by the modulated subcarrier signal.

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15  
16 18. The system of the claim 17, wherein the subcarrier signal is  
17 a squarewave.

18  
19  
20 19. The system of claim 8, wherein the modulator comprises,  
21 a subcarrier generator for generating the subcarrier signal;  
22 a multiplier for multiplying the subcarrier signal by a  
23 modulation index for generating a scaled subcarrier signal;  
24 a scaling mixer for mixing the scaled subcarrier signal with  
25 the encoded subcarrier modulation signal for providing a  
26 modulated subcarrier signal;  
27 a sine and cosine subcarrier processor for receiving the  
28 modulated subcarrier signal for generating a sine subcarrier

1 signal and a cosine subcarrier signal, the sine subcarrier signal  
2 is modulated by the DS data, the cosine subcarrier signal is  
3 unmodulated by the DS data;

4 a carrier phase rotator for combining the sine subcarrier  
5 signal and the cosine subcarrier signal with both of Io encoded  
6 signal and the Qo encoded signal and for providing I and Q  
7 rotated signals, the I rotated signal comprises a scaled Io  
8 encoded signal for communicating the DI data and comprises a  
9 scaled I phase subcarrier signal for communicating the DS data,  
10 the Q rotated signal comprises a scaled Qo encoded signal for  
11 communicating the DQ data and a scaled Q phase subcarrier signal  
12 for communicating the DS data, the scaled I phase and Q phase  
13 subcarrier signals are the I and Q intermodulation products and  
14 are generated when the sine and cosine subcarrier signals are  
15 rotated and combined with Io encoded signal to form the I rotated  
16 signal and when the sine and cosine subcarrier signals are  
17 rotated and combined with the Qo encoded signal to form the Q  
18 rotated signal, the scaled I phase and scaled Q phase subcarrier  
19 signals are orthogonal and are the I and Q intermodulation  
20 products of the Io and Qo encoded signals modulated by harmonics  
21 of the modulated subcarrier signal, the I and Q rotated signals  
22 are scaled by harmonics of the scaled subcarrier signal, the sine  
23 subcarrier signal comprises modulation index scaled, subcarrier  
24 data modulated, odd subcarrier harmonic signals, the cosine  
25 subcarrier signal comprises modulation index scaled even  
26 subcarrier harmonic signals, the modulation index is set to a  
27 predetermined value to weight subcarrier harmonics to set power  
28 of the carrier signal relative to the subcarrier signal while

1 maintaining the constant envelop of the composite signal; and  
2       a quadrature modulator for receiving the I and Q rotated  
3 signals and the carrier signal for respective I and Q phase  
4 modulation of the carrier signal by the I and Q rotated signals  
5 to provide the composite signal having the I phase and Q phase,  
6 the DI data is communicated on the I phase of the composite  
7 signal, the DQ data is communicated on the Q phase of the  
8 composite signal, and the DS data is communicated on both of the  
9 I phase and Q phase of the composite signal, the constant  
10 amplitude envelope results from the I and Q phase modulation of  
11 the carrier signal by the modulated subcarrier signal.

12

13

14 20. The system of claim 19, wherein the modulated subcarrier  
15 signal is equal to the modulation index multiplied by the DS data  
16 by the data partition function by the code partition function by  
17 CS code and by the subcarrier signal.

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## Abstract of the Disclosure

A coherent adaptive subcarrier modulation system applies subcarrier modulation to quadrature modulated signals with constant envelope modulation suitable for efficient sinewave and squarewave subcarrier modulations. The quadrature subcarrier enables the addition of new signals to the in-phase and quadrature phase signals with spectral isolation in the Global Position System while maintaining a constant envelop amplitude.

4. It was discovered just prior to a possible statutory bar date that the co-inventor Tien M. Nguyen was unavailable, by virtue of being out of the U.S., and he is physically unable to sign the oath and assignment for the above referenced patent application in a timely manner.

5. I, the assignee and co-inventor will be prejudiced by an untimely filing of the above referenced patent application, and the application must be filed forthwith in order to preserve patent rights in the claimed invention.

6. The co-inventor should be back in the U.S. within two weeks to execute a supplement oath and the assignment to be filed in the USPTO.

7. I hereby declare that all statements made herein are of my own knowledge and are true, and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment or both under Section 1001 of Title 18 of the United States Code and that such willful false statements may jeopardize the validity of the application or any patent issued thereon.

Date: 5 / 26 1999

  
Philip A. Dafesh

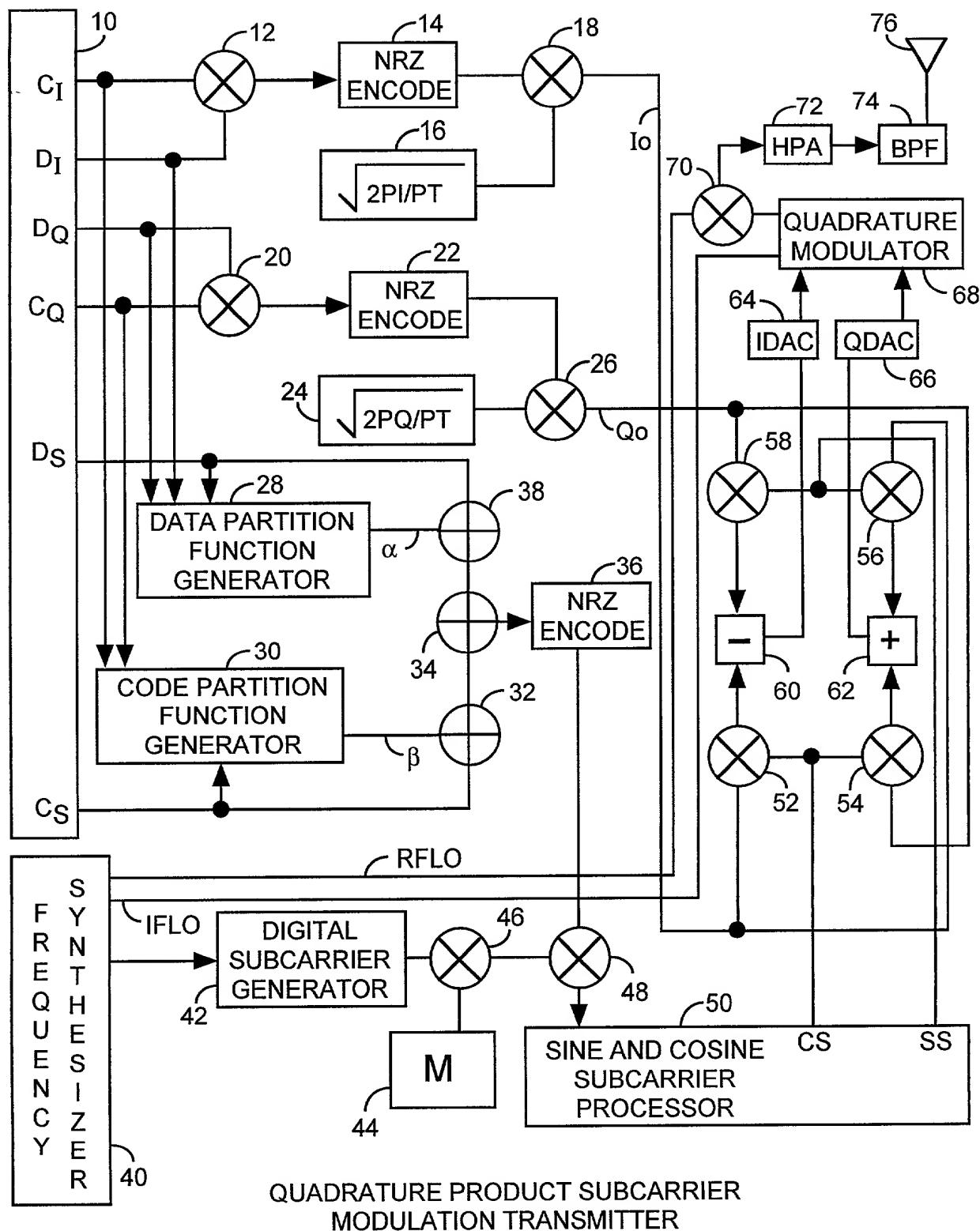
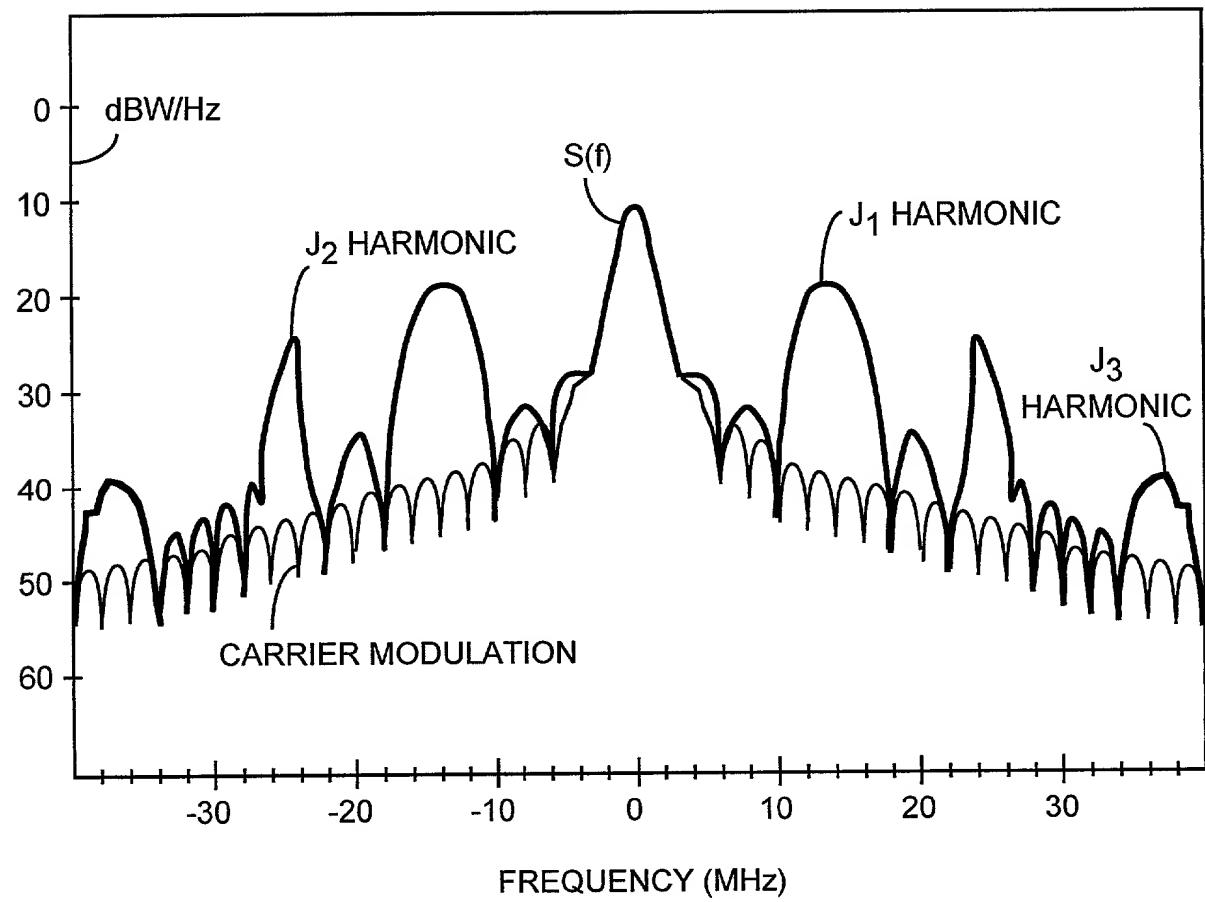
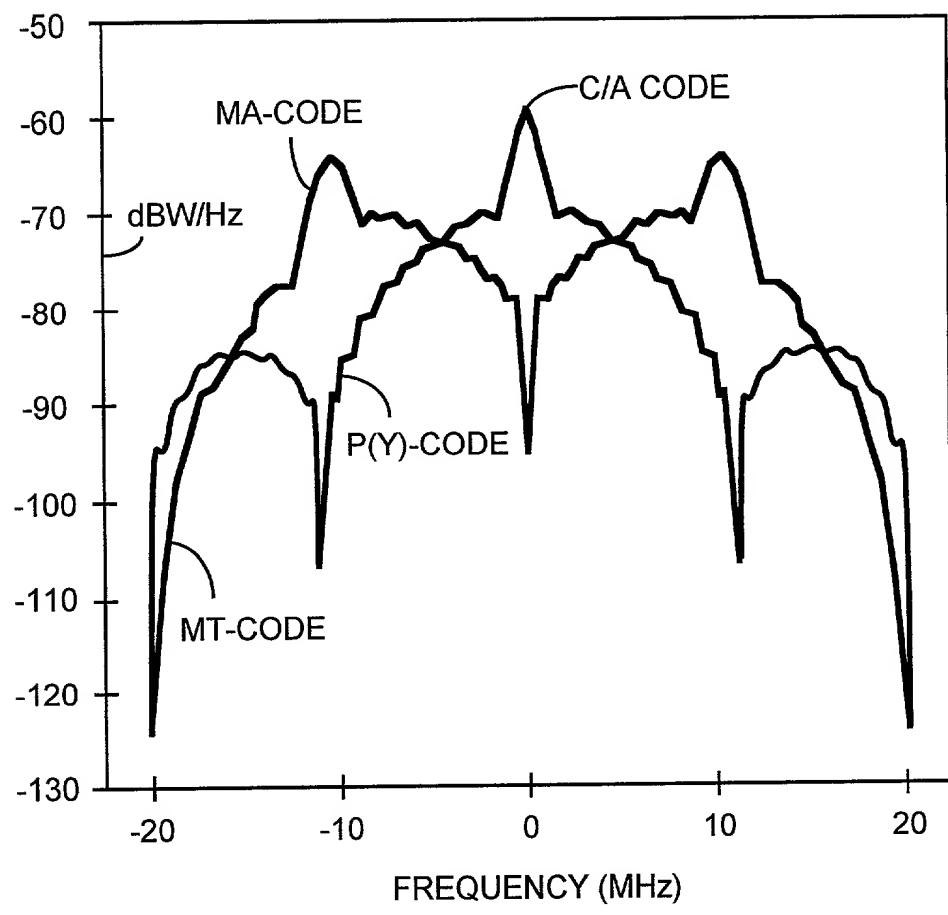


FIG. 1



QPSM POWER SPECTRAL DENSITY

FIG. 2



CASM POWER SPECTRAL DENSITY

FIG. 3

**PATENT**

Attorney's Docket No. D-362

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**COMBINED DECLARATION AND POWER OF ATTORNEY**

---

As a below named inventor, I hereby declare that:

**TYPE OF DECLARATION**

This declaration is of the following type:

/X/ original

**INVENTORSHIP IDENTIFICATION**

My residence, post office address and citizenship are as stated below next to my name, I believe I am the original, first and sole inventor (if only one name is listed below) or an original, first and joint inventor (if plural names are listed below) of the subject matter which is claimed and for which a patent is sought on the invention entitled:

**TITLE OF INVENTION**

---

QUADRATURE PRODUCT SUBCARRIER MODULATION METHOD

---

**SPECIFICATION IDENTIFICATION**

The specification of which is attached hereto.

**ACKNOWLEDGEMENT OF REVIEW OF PAPERS AND DUTY OF CANDOR**

I hereby state that I have reviewed and understand the contents of the above identified specification, including the claims, as amended by any amendment referred to above.

I acknowledge the duty to disclose information which is material to the examination of this application in accordance with Title 37, Code of Federal Regulations section 1.56(a).

/T/ In compliance with this duty there is attached an information disclosure statement. 37 CFR 1.97.

(Declaration & Power of Attorney --page 1 of 2)

**POWER OF ATTORNEY**

As a named inventor, I hereby appoint the following attorney(s) and/or agents(s) to prosecute this application and transact all business in the Patent and Trademark Office connected therewith:

Derrick Michael Reid, Reg. No. 32,096

**SEND CORRESPONDENCE TO:**

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**DIRECT TELEPHONE CALLS TO:**

Derrick M. Reid  
(310) 336-6708

**DECLARATION**

I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both under Section 1001 of Title 18 of the United States Code and that such willful false statements may jeopardize the validity of the application or any patent issued thereon.

**SIGNATURE(S)**

Full name of sole or first inventor: Philip A. Dafesh

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Date: 5-26-99 Country of Citizenship: U.S.A.

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Full name of third joint inventor, if any: \_\_\_\_\_

Inventor's signature: \_\_\_\_\_

Date: \_\_\_\_\_ Country of Citizenship: \_\_\_\_\_

Residence: \_\_\_\_\_

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X This Declaration ends with this page-- page 2 of 2)

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In the United States Patent Office  
Before the Assistant Commissioner of Patents

Inventors: Philip A. Dafesh )  
                               )  
                               ) Declaration of Philip A. Dafesh  
Title: Quadrature Product   ) in lieu of Oath of the Co-inventor  
Subcarrier Modulation    )  
System                      )  
                              )  
                              )  
Docket No. D-362           )

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Assistant Commissioner of Patents  
Washington, DC 20231

Declaration

I, Philip A. Dafesh, do hereby declare and state:

1. I am a co-inventor of assignee, The Aerospace Corporation, located at 2350 East El Segundo Blvd, El Segundo, California 90245-4691, and I am authorized to execute this declaration on behalf of the assignee.

3. Co-inventor Mr. Tien M. Nguyen is also an employee of assignee, and his home address is 433 Swanson Avenue, Placentia, California, 92870.